# Material transport in the frame of PSI

K. Krieger

with contributions from many colleagues (credits inside)

Association EURATOM Max-Planck Institut für Plasmaphysik, Boltzmannstr. 2, 85748 Garching, Germany



K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009





K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009



# What are the consequences of material migration?



IPP

#### **Deposited layers may form ever growing inventory of buried fuel!**

# What happens if deposited layers become too thick?

IPP

![](_page_6_Picture_1.jpeg)

#### Negative consequences of material mixing?

![](_page_7_Picture_1.jpeg)

#### YES! Example: beryllium and tungsten can form alloys

![](_page_7_Figure_3.jpeg)

![](_page_8_Figure_0.jpeg)

## Key questions of material (impurity) transport

For given impurity edge density, what is the impurity density in the plasma centre? or What is the impurity residence time compared to the fuel ion residence time in the plasma? IPP

**Core transport coefficients** 

For given material erosion source, how much gets into the confined plasma?

Screening factor, divertor retention

Where are eroded impurities re-deposited?

**Migration paths** 

## Impurity transport $\perp$ B by particle collisions

![](_page_10_Picture_1.jpeg)

#### **Particle conservation**

$$\frac{\partial n_{I,Z}}{\partial t} = -\boldsymbol{\nabla} \cdot \boldsymbol{\Gamma}_{I,Z} + Q_{I,Z}$$

lons bound to flux surface

 $\langle n_I \rangle = n_I$ 

i.e. densities constant on flux surface

![](_page_10_Figure_7.jpeg)

Impurity density is only a function of flux surface label  $r=\sqrt{V/(2\pi^2R_0)}$ 

and flux is described by diffusion + convection

$$\frac{\partial n_{I,Z}}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} r \left( D^* \frac{\partial n_{I,Z}}{\partial r} - v^* n_{I,Z} \right) + Q_{I,Z}$$

**Fransport coefficients ⇒ averages over flux surface** 

#### Impurity transport $\perp$ B by particle collisions

![](_page_11_Picture_1.jpeg)

$$D = D^{CL} + D^{PS} + D^{BP}$$

$$D^{CL} \cong \frac{m_I k T v_{ID}}{B_0^2 e^2 Z^2} \propto \frac{1}{\sqrt{T} B_0^2 Z^2}$$

Classical transport due to collisional friction forces  $\perp B$ 

 $D^{PS} \cong 2q^2 D^{CL} \propto \frac{1}{\sqrt{T}B_p^2 Z^2}$ 

Pfirsch-Schlüter transport due to collisional friction forces || B

 $D^{BP} \cong \frac{q^2}{\varepsilon^2} \frac{kT\mu_{ID}^*}{B_0^2 e^2 Z n_I} \propto \frac{1}{\sqrt{T}B^2 Z n_I}$ 

Banana-Plateau transport due to viscosity forces || B

 $\mathcal{E} = \frac{r}{R_0}$ 

 $q = \varepsilon \frac{B_T}{B_F}$ 

Impurity transport  $\perp$  B by particle collisions

![](_page_12_Picture_1.jpeg)

$$\mathbf{V}^{XX} = D^{XX} Z \left( \frac{d \ln n_D}{dr} + H^{XX} \frac{d \ln T}{dr} \right)$$

All drifts have the same form but the sign of *H<sup>xx</sup>* may change!

IPP

#### Why is this important?

$$\frac{d\ln n_Z}{dr} = Z \frac{d\ln n_I}{dr} \left( 1 + \frac{H_{eff}}{dr} \frac{d\ln T}{dr} / \frac{d\ln n_I}{dr} \right)$$

► Temperature screening factor 🗢 generally negative!

Pure neoclassical transport leads to central impurity peaking Peaked temperature profile alleviates problem

#### Is transport really only due to collisions?

![](_page_13_Picture_1.jpeg)

IPP

![](_page_13_Figure_2.jpeg)

#### NO: "Anomalous diffusion" generally much larger!

![](_page_14_Picture_1.jpeg)

$$\frac{d\ln n_Z}{dr} = Z \frac{d\ln n_I}{dr} \left(1 + H_{eff} \frac{d\ln T}{dr} / \frac{d\ln n_I}{dr}\right) \left(\frac{D}{D + D_{AN}}\right)$$

IPΡ

**GOOD!**  $D_{AN}$  decreases impurity profile peaking Also holds for fuel ions so that  $d \ln n_I / dr$ 

#### **Purely collisional transport**

![](_page_15_Picture_1.jpeg)

R. Dux

#### Discharge with quiescent plasma

![](_page_15_Figure_3.jpeg)

#### Impurity peaking in centre according to neoclassical D and v

# What are the origins of "anomalous" transport?

# Large scale MHD instabilities create radial "shortcut"

![](_page_16_Figure_2.jpeg)

IPP

#### Not the whole story: Anomalous diffusion shows also in absence of MHD instabilities

Turbulence, carrying impurities with it!

#### **Turbulent processes in a Tokamak plasma?**

Plasma temperature

![](_page_17_Picture_1.jpeg)

F. Jenko

![](_page_17_Picture_2.jpeg)

ASDEX Upgrade

K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009

Plasma density

K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009

**Vlasov-Maxwell equations** 

Ab initio model of plasma microturbulence ⇒ nonlinear gyrokinetic theory

Hot fusion plasmas are almost collisionless (even in the edge!)

Eliminating the fast gyromotion...

(self-consistent, nonlinear problem)

[Frieman, Chen, Lee, Hahm, Brizard *et al*. in the 1980s]

Charged rings as quasiparticles; important kinetic effects retained non-perturbatively!

✤Irrelevant (small) spatio-temporal scales are removed!

 $\omega \ll \Omega$ 

$$\underbrace{\mathbf{v}_{E} + \mathbf{v}_{\kappa} + \mathbf{v}_{\nabla B}}_{\mathbf{v}_{E}}$$

$$\left[\frac{\partial}{\partial t} + \mathbf{v} \cdot \frac{\partial}{\partial \mathbf{x}} + \frac{q}{m} \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B}\right) \cdot \frac{\partial}{\partial \mathbf{v}}\right] f(\mathbf{x}, \mathbf{v}, t) = 0$$

![](_page_18_Picture_10.jpeg)

F. Jenko

## The nonlinear gyrokinetic equations

![](_page_19_Picture_1.jpeg)

 $f = f(\mathbf{X}, v_{\parallel}, \mu; t)$ 

advection equation/conservation law

$$\frac{\partial f}{\partial t} + \dot{\mathbf{X}} \cdot \frac{\partial f}{\partial \mathbf{X}} + \dot{v}_{\parallel} \frac{\partial f}{\partial v_{\parallel}} = 0$$

$$\dot{\mathbf{X}} = v_{\parallel} \mathbf{b} + \frac{B}{B_{\parallel}^*} \left( \frac{v_{\parallel}}{B} \bar{\mathbf{B}}_{1\perp} + \mathbf{v}_{\perp} \right)$$

 $\mathbf{v}_{\perp} \equiv \frac{c}{B^2} \bar{\mathbf{E}}_1 \times \mathbf{B} + \frac{\mu}{m\Omega} \mathbf{b} \times \nabla (B + \bar{B}_{1\parallel}) + \frac{v_{\parallel}^2}{\Omega} (\nabla \times \mathbf{b})_{\perp}$ 

**X** = position of the gyrocenter

 $\mu$  = magnetic moment

#### F. Jenko

#### **Corresponding field equations**

$$\frac{n_1}{n_0} = \underbrace{\bar{n}_1}_{n_0} - \left(1 - \|I_0^2\|\right) \frac{e\phi_1}{T} + \|xI_0I_1\| \frac{B_1\|}{B}$$

$$\nabla_{\perp}^2 A_{1\parallel} = -\frac{4\pi}{c} \sum \bar{J_{1\parallel}}$$

$$\dot{v}_{\parallel} = \frac{\dot{\mathbf{X}}}{mv_{\parallel}} \cdot \left(e\bar{\mathbf{E}}_{1} - \mu\nabla(B + \bar{B}_{1\parallel})\right) \qquad \qquad \frac{B_{1\parallel}}{B} = -\sum \epsilon_{\beta} \left(\frac{\bar{p}_{1\perp}}{n_{0}T} + \|xI_{1}I_{0}\|\frac{e\phi_{1}}{T} + \|x^{2}I_{1}^{2}\|\frac{B_{1\parallel}}{B}\right)$$

#### Nonlinear integro-differential equations in 3+2 dimensions

# Progress only recently due to complexity of the system

# Plasma turbulence is quasi-two-dimensional Work with flux tubes, using field-aligned coordination Ð Still requires O(100000) CPU-hours!

F. Jenko

IPP

IPP

#### B-field intersects material surface **\***transport II B becomes important!

![](_page_21_Figure_3.jpeg)

#### Is that the whole story?

![](_page_22_Picture_1.jpeg)

![](_page_22_Figure_2.jpeg)

#### How to improve the quasi 1D-model?

![](_page_23_Picture_1.jpeg)

Kinetic equations  $\rightarrow$  Moments of ion and electron distribution functions  $\rightarrow$  Fluid equations (Braginskii)

Particle balance		
Momentum balance		<ul> <li>Kinetic correction terms (flux limiters)</li> <li>Self consistent treatment of recycling by iterative coupling to neutral transport code</li> </ul>
Diffusion	PLUS	
Electron energy balance		
Ion energy balance		

# **Standard used for ITER: B2-EIRENE**

#### **Example solution for ITER plasma**

![](_page_24_Picture_1.jpeg)

![](_page_24_Figure_2.jpeg)

#### **Example solution for ITER plasma**

![](_page_25_Picture_1.jpeg)

![](_page_25_Figure_2.jpeg)

#### How to benchmark the codes?

![](_page_26_Picture_1.jpeg)

# **Challenge with experimental data**

![](_page_27_Figure_0.jpeg)

K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009

![](_page_28_Picture_1.jpeg)

Quantify material erosion and redeposition by ex-situ surface analysis of retrieved wall tiles and/or long term probes

Identification of erosion and deposition dominated areas Identification of net material migration balance

![](_page_29_Picture_1.jpeg)

![](_page_29_Picture_2.jpeg)

![](_page_29_Picture_3.jpeg)

#### M. Mayer

![](_page_30_Picture_1.jpeg)

#### Carbon deposition in the inner divertor of ASDEX Upgrade

M. Mayer

![](_page_30_Figure_4.jpeg)

![](_page_30_Picture_5.jpeg)

- Decrease of C-deposition on divertor tiles by factor 7 after W coverage of outer limiters
- No change in outer divertor erosion
- Outboard limiters identified as main carbon source

![](_page_30_Picture_9.jpeg)

Carbon deposition / erosion in lower divertor of ASDEX Upgrade

![](_page_31_Picture_1.jpeg)

IPP

#### Discharge time [s] 98' 9A 6A 6B 9Ĉ. 600 400 200 0 ---- B+C 6 Erosion/Deposition 2 10<sup>19</sup> at./cm<sup>2</sup> **Deposition** in 0 inner divertor -2 **Erosion** in -6 outer divertor -8 200 400 600 800 1000 1200 1400 0 s-coordinate [mm]

![](_page_32_Picture_1.jpeg)

#### Tungsten deposition / erosion in lower divertor of ASDEX Upgrade

![](_page_32_Figure_3.jpeg)

![](_page_33_Figure_0.jpeg)

#### **Summary**

![](_page_34_Picture_1.jpeg)

Advantages:

Independent of experiment programme Possible to survey large vessel areas

**Disadvantages:** 

Integral over many plasma scenarios makes interpretation and code benchmarking difficult

![](_page_35_Picture_1.jpeg)

Inject tracer material in discharges at the end of an experimental campaign

Quantify tracer deposition by ex-situ surface analysis of retrieved wall tiles and/or long term probes

Identification of net material migration path (locally or globally) for particular discharge scenario

# **Example: 13CH4 injection in ASDEX Upgrade**

![](_page_36_Picture_1.jpeg)

IPP

**Observed deposition pattern determined by both plasma flow and by geometry** 

#### **Example: 13CH4 injection in JET**

![](_page_37_Picture_1.jpeg)

IPP

J. Strachan

#### Benchmarking EDGE2D fluid code model

# **Example: 13CH4 local injection in ASDEX Upgrade**

![](_page_38_Figure_1.jpeg)

IPP

□ Puff trace amounts of <sup>13</sup>CD<sub>4</sub> in series of similar discharges and measure local <sup>13</sup>C deposition 2D-distribution at retrieved tiles.
 ▷ Benchmark data for ERO and for spectroscopic CD flux

#### IPP **Example: 13CH4 local injection in ASDEX Upgrade** gnetic pitch angle: 1 deg 1250 5 deg 2 dea Poloidal S coordinate [mm] - 6 dea 11 L-mode discharges 1200 gnetic pitch angle: 1 deg <sup>13</sup>CH<sub>4</sub> puff 1.6–4.6 s 0 dea 1150 **Reversal of deposition shift at** Separatrix 10 <sup>16</sup> at/cm **B-field reversal** -50 0 50 100 Toroidal coordinate [mm] **♦** Shift due to ExB drift 1250 Poloidal S coordinate [mm] 3 L-mode discharges <sup>13</sup>CH<sub>4</sub> puff <u>1.6−4.3 s</u> □ Reversed B<sub>t</sub>, I<sub>p</sub> 1.5E3 1.0E3 6.3E2 4.0E2 2.5E2 1.5E2 1.0E2 n<sub>13c</sub> [10<sup>15</sup>at/cm<sup>2</sup>] 1100 -50 100 0 50 Toroidal coordinate [mm]

K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009

#### **Example: 13CH4 local injection in ASDEX Upgrade**

![](_page_40_Figure_1.jpeg)

IPP

![](_page_41_Picture_1.jpeg)

#### Advantages:

Well defined particular discharge scenario for code benchmarking Very sensitive quantification of tracer materials

#### **Disadvantages:**

Provides only net-deposition data. Re-erosion only by indirect evidence

Only one scenario per campaign

![](_page_42_Picture_1.jpeg)

Cover main chamber wall with Be by heavy Be evaporation.

Follow relaxation of Be/C wall sources, plasma concentration and QMB deposition towards steady state situation.

**Compare to reference discharge immediately before Be evaporation.** 

Spectroscopic measurements allow to determine gross erosion flux.

Allows to study global screening by comparison with plasma impurity concentration.

**Evolution of wall composition provides information on material migration.** 

#### **Diagnostic array**

![](_page_43_Picture_1.jpeg)

![](_page_43_Figure_2.jpeg)

#### **Evolution of Be wall sources**

![](_page_44_Picture_1.jpeg)

![](_page_44_Figure_2.jpeg)

## **Evolution of Be divertor sources**

![](_page_45_Picture_1.jpeg)

![](_page_45_Figure_2.jpeg)

# Modelling wall composition change by migration

![](_page_46_Figure_1.jpeg)

IPP

![](_page_47_Picture_1.jpeg)

Advantages: Well defined particular discharge scenario for code benchmarking Trace several materials simultaneously

**Disadvantages:** 

Provides only gross erosion data. Deposition only by indirect evidence

**Quantitative impurity flux quantification requires** local plasma parameters

![](_page_48_Picture_1.jpeg)

#### Direct observation of impurity radiation during injection

Spectroscopic measurements allow to determine spatial distribution of emission by successive ionisation states

Allows to directly observe the influence of transport

# **Example: carbon flow measurements in DIII-D**

![](_page_49_Picture_1.jpeg)

- Principal flow measurements in the plasma crown
  - Multi-tipped, reciprocating Langmuir probe: parallel-B v<sub>D+</sub>

IPP

- Passive Doppler spectroscopy: parallel-B v<sub>C+</sub>, v<sub>C2+</sub>
- Toroidally symmetric injection of CH<sub>4</sub> from lower outer pumping plenum + tangential cameras
  - Emission profiles: direction of low charge-state carbon flow
  - Order-of-magnitude estimate of C<sup>+</sup> poloidal velocity

#### M. Groth

#### **Example: carbon flow measurements in DIII-D**

# Carbon emission profiles of CH4 break-up are progressively shifted radially inward and poloidally toward inner plate

IPP

![](_page_50_Figure_2.jpeg)

K. Krieger, 3rd ITER Summer School, Aix-en-Provence, 24.06.2009

![](_page_51_Figure_0.jpeg)

#### Outlook

![](_page_52_Picture_1.jpeg)

#### **Experiment side**

Implement new PSI and impurity transport diagnostics to study timedepent processes in single discharges

Improve diagnostics for characterisation of incident plasma flux

**Modelling side** 

Get complete treatment of transport processes

Coupled codes for plasma and material side

Extend computational domain for plasma towards entire 1st wall

**Develop 3D codes for near wall domain**